

Simplify

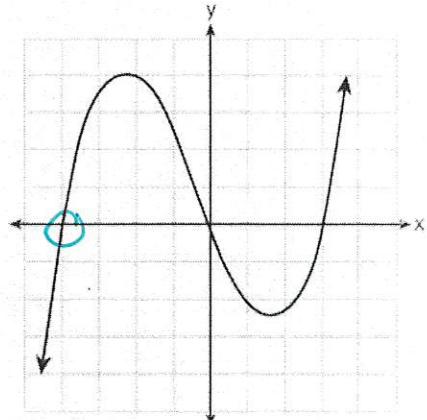
- Polynomials
- Radicals
- Powers of i
- Trig
- Trig identities
- Exponent rules
- Average rate of change
- Rational expressions
- Circles

1. The graph of $p(x)$ is shown. What is the remainder when $p(x)$ is divided by $x + 4$? → FACTOR

- a. $x - 4$
b. -4

Root → -4
SINCE -4 IS A
ROOT FROM THE
GRAPH, THE
REMAINDER IS ZERO.

- c. 0
d. 4



2. Write $\sqrt[3]{x} \cdot \sqrt{x}$ as a single term with a rational exponent.

$$(x)^{\frac{1}{3}}(x)^{\frac{1}{2}} \rightarrow x^{\frac{1}{3} + \frac{1}{2}} \rightarrow x^{\frac{5}{6}} \rightarrow \sqrt[6]{x^5}$$

3. If $\sin^2(32) + \cos^2(x) = 1$, then what does x equal?

- a. 72
b. 68

PYTHAGOREAN
IDENTITY ...
 $\sin^2 x + \cos^2 x = 1$
SAME → $x = 32$

- c. 58
d. 32

4. Over the set of integers, factor $4x^3 - x^2 + 16x - 4$ completely.

4 TERMS → FACTOR BY GROUPING

$$\begin{aligned} & \underline{4x^3 - x^2} + \underline{16x - 4} \\ & x^2(4x - 1) + 4(4x - 1) \\ & (4x - 1)(x^2 + 4) \end{aligned}$$

5. Simplify $xi(x - 5i)^2$, where i is the imaginary unit.

$$\begin{aligned}
 & \overbrace{x_i(x-s_i)(x-s_i)}^{\text{Reduction}} \\
 & x_i \cancel{(x^2 - 10x_i + 25i^2)} \\
 & \cancel{x_i^3} - 10x_i^2 + 25x_i^3
 \end{aligned}
 \quad
 \begin{aligned}
 & \overbrace{x^3(-10x^2(-1) + 25x(-i))}^{\text{Expansion}} \\
 & x^3 + 10x^2 - 25xi
 \end{aligned}$$

6. Use an appropriate procedure to show that $x - 4$ is a factor of $f(x) = 2x^3 - 5x^2 - 11x - 4$. Explain your reasoning. $X-4 \rightarrow \text{use } 4 \text{ for synthetic division.}$

$$\begin{array}{r}
 & \text{---} \\
 4 | & 2 & -5 & -11 & -4 \\
 & \downarrow & & & \\
 & 8 & 12 & 4 \\
 \hline
 & 2 & 3 & 1 & 0
 \end{array}$$

SINCE THE REMAINDER
IS 0, $x-4$ IS A FACTOR
OF $f(x)$.

7. Write $(4 + 3yi)(2 - 5i) - (4 - 3yi)(2 - 5i)$ in $a + bi$ form, where y is a real number.

$$\begin{aligned}
 & (8 - 20i + 6yi - 15y^2) - (8 - 20i - 6yi + 15y^2) \\
 & (8 - 20i + 6yi + 15y) - (8 - 20i - 6yi - 15y) \\
 & 8 - 20i + 6yi + 15y - 8 + 20i + 6yi + 15y \\
 & 12yi + 30y \\
 & 30y + 12yi
 \end{aligned}$$

8. Which is a binomial factor of $x^4 - 4x^2 - 4x + 8$?

- a. $x - 2$
 - b. $x + 2$

$$\begin{aligned} & x^2(x^2 - 4) - 4(x-2) \\ & x^2(x-2)(x+2) - 4(x-2) \\ & (x-2)(x^2(x+2) - 4) \end{aligned}$$

- c. $x - 4$
d. $x + 4$

* OR GRAPH AND USE TABLE TO VERIFY
THE ROOT EQUALS ZERO.

9. Express $(3b)^{\frac{d}{2}}$ in radical form.

$$\sqrt[3]{(3b)^d}$$

10. Given: $f(x) = 2x^2 + x - 3$ and $g(x) = x - 1$. Express $f(x) \cdot g(x) - [f(x) + g(x)]$ as a polynomial in standard form.

$$(2x^2 + x - 3)(x - 1) - [(2x^2 + x - 3) + (x - 1)]$$

	$2x^2$	x	-3
x	$2x^3$	x^2	$-3x$
-1	$-2x^2$	$-x$	$+3$

$$2x^3 - x^2 - 4x + 3 - [2x^2 + 2x - 4]$$

$$2x^3 - x^2 - 4x + 3 - 2x^2 - 2x + 4$$

$$2x^3 - 3x^2 - 6x + 7$$

$$2x^3 - x^2 - 4x + 3$$

11. Which function, $f(x)$ or $g(x)$, has a greater average rate of change on the interval $[-2, 4]$? Justify your answer.

$g(x)$ (FROM TABLE WITH CALCULATOR)

$$\begin{array}{l} (-2, -49) \\ (4, 179) \end{array} \left\{ \begin{array}{l} 179 - (-49) \\ 4 - (-2) \end{array} \right.$$

$$[38]$$

$$g(x) = 4x^3 - 5x^2 + 3$$

$g(x)$ HAS A GREATER AVERAGE RATE OF CHANGE.

$$\begin{array}{l} f(x) \\ (-2, 1.25) \\ (4, 80) \end{array} \left\{ \begin{array}{l} 80 - 1.25 \\ 4 - (-2) \end{array} \right.$$

$$[13.125]$$

x	f(x)
-4	0.3125
-3	0.625
-2	1.25
-1	2.5
0	5
1	10
2	20
3	40
4	80
5	160
6	320

12. Factor $2d^4 + 6d^3 - 18d^2 - 54d$ completely.

$$2d^3(d+3) - 18d(d+3)$$

$$(d+3)(2d^3 - 18d)$$

$$(d+3)(2d)(d^2 - 9)$$

$$(d+3)(2d)(d+3)(d-3)$$

13. The equation $4x^2 - 24x + 4y^2 + 72y = 76$ is equivalent to

a. $4(x - 3)^2 + 4(y + 9)^2 = 76$

b. $4(x - 3)^2 + 4(y + 9)^2 = 121$

c. $4(x - 3)^2 + 4(y + 9)^2 = 166$

d. $4(x - 3)^2 + 4(y + 9)^2 = 436$

$$4x^2 - 24x + \underline{\quad} + 4y^2 + 72y + \underline{\quad} = 76 + \underline{\quad} + \underline{\quad}$$

$$4(x^2 - 6x + 9) + 4(y^2 + 18y + 81) = 76 + 36 + 324$$

$$4(x-3)^2 + 4(y+9)^2 = 436$$

*9 because $(\frac{6}{2})^2$, 36 because $4(9) = 36$

*81 because $(\frac{18}{2})^2$, 324 because $4(81) = 324$

14. When $g(x)$ is divided by $x + 3$, the remainder is 0. What can you state about $g(-3)$?

IF THE REMAINDER IS 0, THEN $x+3$ IS A FACTOR.

IF $x+3$ IS A FACTOR, THEN $x=-3$ IS A ROOT.

IF $x=-3$ IS A ROOT, THEN $g(-3)$ EQUALS 0.

15. Which binomial is NOT a factor of $x^3 - 11x^2 + 16x + 84$?

a. $x + 2 \rightarrow$ SUB $x = -2 \rightarrow y = 0$ FACTOR

b. $x + 4 \rightarrow$ SUB $x = -4 \rightarrow y = -22$ NOT

c. $x - 6 \rightarrow x = 6 \rightarrow y = 0$ FACTOR

d. $x - 7 \rightarrow x = 7 \rightarrow y = 0$ FACTOR

16. Simplify $(-8)^{\frac{4}{3}}$. Explain your steps.

$$\sqrt[3]{(-8)^4} \\ (-2)^4 \\ 16$$

FIRST I RE-WROTE AS A CUBE ROOT WITH A FOURTH POWER. THEN I EVALUATED THE CUBE ROOT TO GET -2. LASTLY, I EVALUATED THE FOURTH EXPONENT.

17. Simplify $\frac{4x^3 + 5x + 10}{2x + 3} = 2x^2 - 3x + 7 - \frac{11}{2x + 3}$

$$2x+3 \overline{)4x^3 + 0x^2 + 5x + 10} \\ - (4x^3 + 6x^2) \\ \underline{-6x^2 + 5x} \\ - (-6x^2 - 9x) \\ \underline{+14x + 10} \\ - (+14x + 21) \\ \underline{-11}$$

18. Factor $m^5 + m^3 - 6m$ completely.

$$M(M^4 + M^2 - 6)$$

$$M(M^2 + 3)(M^2 - 2)$$

19. Which expression has been rewritten correctly to form a true statement?

- a. $(x+2)^2 + 2(x+2) - 8 = (x+6)x$
- b. $x^4 + 4x^2 + 9x^2y^2 - 36y^2 = (x+3y)^2(x-2)^2$
- c. $x^3 + 3x^2 - 4xy^2 - 12y^2 = (x-2y)(x+3)^2$
- d. $(x^2 - 4)^2 - 5(x^2 - 4) - 6 = (x^2 - 7)(x^2 - 6)$

STORE VALUES
FOR X & Y
AND CHECK!

20. When is the function $f(x) = \frac{x-3}{x^2+2x-8}$ undefined?

UNDEFINED WHEN

$$x^2 + 2x - 8 = 0$$

$$x = -4 \text{ or } x = 2$$

$$(x+4)(x-2) = 0$$

$$x+4=0 \text{ or } x-2=0$$

$$x = -4 \text{ or } x = 2$$

21. Divide $\frac{x^3+2x^2+x+6}{x+2} = x^2 + 0x + 1 + \frac{4}{x+2}$

$$\begin{array}{r} \overline{-2 \Big| 1 \quad 2 \quad 1 \quad 6} \\ \downarrow \quad -2 \quad 0 \quad -2 \\ 1 \quad 0 \quad 1 \quad 4 \end{array}$$

22. Simplify $\frac{-3x^2-5x+2}{x^3+2x^2}$

$$\begin{aligned} &\frac{-3(-2)}{x^3+2x^2} = -6, \text{ so } \dots \frac{3x^2+6x-1}{x-2} \\ &\frac{-1(3x^2+5x-2)}{x^2(x+2)} \rightarrow \frac{-1(x+2)(3x-1)}{x^2(x+2)} \rightarrow -\frac{3x-1}{x^2} \\ &\text{OR } \frac{-1(3x-1)}{x^2} \rightarrow \frac{-3x+1}{x^2} \end{aligned}$$

23. What is the quotient when $10x^3 - 3x^2 - 7x + 3$ is divided by $2x - 1$?

- a. $5x^2 + x + 3$
- b. $5x^2 - x + 3$

$$\begin{array}{r} \overline{2x-1 \Big| 10x^3 - 3x^2 - 7x + 3} \\ \underline{- (10x^3 - 5x^2)} \\ \overline{2x^2 - 7x} \\ \underline{- (2x^2 - x)} \\ \overline{- 6x + 3} \\ \underline{- (-6x + 3)} \\ \overline{0} \end{array}$$

- c. $5x^2 - x - 3$
- d. $5x^2 + x - 3$