

Examples:

$$\textcircled{1} \quad x^4 \cdot x^2 y^3 = x^6 y^3$$

$$\textcircled{2} \quad \frac{(4x)^3}{4x^3} = \frac{64x^3}{4x^3} = 16$$

$$\textcircled{3} \quad \frac{x^2(y^3z)^3}{(x^2y)^2z} = \frac{x^2y^9z^3}{x^4y^2z} = \frac{y^7z^2}{x^2}$$

$$\textcircled{4} \quad (2y^4)^3 = 8y^{12}$$

$$\textcircled{5} \quad \frac{3(x^3)^4 y^5}{3x^7} = \frac{3x^{12} y^5}{3x^7} = x^5 y^5$$

$$\textcircled{6} \quad \frac{y^4}{y^0} = y^4$$

$$\textcircled{7} \quad -(3x^3)^2 = -9x^6$$

\textcircled{8} If $a = 3$ and $b = -2$, what is the value of the expression $\frac{a^{-2}}{b^{-2}}$?

$$\frac{b^3}{a^2} = \frac{(-2)^3}{(3)^2} = -\frac{8}{9}$$

$$\textcircled{9} \quad \frac{a^2 b^{-3}}{a^{-4} b^2} = \frac{a^2 \cdot a^4}{b^2 \cdot b^3} = \frac{a^6}{b^5}$$

$$\textcircled{10} \quad 8^{-4} \cdot 8^6 = 8^2 = 64$$

$$\textcircled{11} \quad \text{Simplify the expression } \frac{3x^{-4}y^5}{(2x^3y^{-7})^{-2}} \text{ and write the answer using only positive exponents.}$$

$$\frac{3x^{-4}y^5}{2^{-2}x^{-6}y^{14}} = \frac{3 \cdot 2^2 \cdot x^6 \cdot y^5}{x^4 y^{14}} = \frac{12x^2}{y^9}$$

$$\textcircled{12} \quad \text{In simplest form, express } \frac{x+y^{-1}}{y+x^{-1}} \text{ with no negative exponents.}$$

$$\begin{aligned} \frac{x+\frac{1}{y}}{\frac{y}{x}+1} &\rightarrow \frac{\frac{xy+1}{y}}{\frac{y}{x}+1} = \frac{xy+1}{y} \cdot \frac{x}{xy+1} = \frac{x}{y} \end{aligned}$$